

Chapter 5

Lagrangian Dynamics of Manipulators

Sandipan Bandyopadhyay
Indian Institute of Technology Madras, India

ABSTRACT

Service robots can be thought of as having two types of motion: (a) locomotion of the entire robot, which can be either legged or wheeled, and (b) motion of the manipulator limbs, e.g., object manipulation by the “hands” etc. While the first type is very specialised, in particular in the case of legged motion, the second is fairly generic and can be discussed in detail without making a very heavy demand on the mathematical background of the reader. With that in mind, in the following, the author considers the dynamics of two types of systems, which are known as serial or open-loop, and parallel or closed-loop manipulators. The examples of these would be the hands of a humanoid robot, when considered in isolation, and when clasped together or holding an object with both hands, respectively. The examples considered here would be planar in order to keep them simple; however, the formulation presented would be general, so that the reader can, very easily, use it to model and simulate spatial manipulators.

INTRODUCTION

The purpose of this chapter is to familiarise the reader with the basics of modelling the dynamics of a robot manipulator. The framework of Lagrangian mechanics is used. The reader is expected to be

conversant with the basics of robot kinematics to the extent of using Jacobian matrices in describing the velocities of various points on a robot. The fundamentals of such an approach can be found in standard textbooks, such as Craig (1986), Ghosal (2006), and Saha (2008).

The study of dynamics of a robot (or any mechanical system for that matter) can be divided into two main categories:

- Forward dynamics: This is the study of the robot's response to a given set of inputs, i.e., forces/moments applied by the actuators at the various joints. This mode of analysis commonly forms the backbone of the synthesis of suitable control schemes for the robots, as one needs to ascertain the control responses first in simulations before applying them to the actual robot.
- Inverse dynamics: In this mode of analysis, the robot's motion is specified, and the actuation forces¹ required to *cause* the motion are computed. The major utility of this analysis is in sizing up appropriate actuators, and also finding out various forces in the manipulator's links and joints that are needed for the detailed mechanical design of the manipulator, i.e., the physical dimensions of the links and joints.

As we shall see in the following, at the level of modelling the above distinction is only notional. It is only in the simulations one can choose between the modes.

FORMULATION OF THE EQUATION OF MOTION

The most important part of a study in dynamics is the derivation of the equation of motion. It is also known as *modelling of the system*, since it is the process of abstracting a mechanical system in terms of mathematical equations. Obviously, this can only be achieved (without getting into too many of the complications) if certain idealisations are incorporated in the model. The usual ones are obvious:

1. The links are rigid.
2. The joints are ideal.
3. All the geometry and inertia parameters are known accurately.
4. Frictional, as well as other disturbance forces, are either absent or their behavior is known accurately enough to be incorporated in the model.

We assume all of the above in the following. However, the reader should note that more sophisticated analysis, known as system identification, can obviate the need of the last two assumptions to some extent. Further, there is a class of robots known as flexible manipulators where the first assumption is not warranted, and the joints may not even be present!

The Lagrangian Approach to Dynamics

The reader should be familiar with at least one of the various approaches to dynamics, namely, the Newton-Euler approach. Before embarking on the discussion of Lagrangian dynamics, a brief comparison of it with the former may be in order.

The concept of *Free-Body Diagrams* (FBDs) is at the heart of Newtonian mechanics. As one can see in Figure 1, when a multi-body system is to be analysed, one decomposes it (notionally) into a set of rigid bodies, thereby bringing into the picture *action-reaction pairs*, namely, the joint reactions. The set of dynamic equations are written for each component, and then the set of reactions are eliminated from them systematically, to finally lead to the equation of motion for the *system*. This approach is rather appealing from a physical standpoint, since it directly concerns physical entities such as forces and accelerations, i.e., there are no abstract concepts to be dealt with in this approach. However, from an analysis perspective, it poses several challenges:

12 more pages are available in the full version of this document, which may be purchased using the "Add to Cart" button on the product's webpage:

www.igi-global.com/chapter/lagrangian-dynamics-manipulators/64660?camid=4v1

This title is available in InfoSci-Books, InfoSci-Software Technologies, Science, Engineering, and Information Technology, InfoSci-Select, InfoSci-Engineering Science and Technology, InfoSci-Select. Recommend this product to your librarian:

www.igi-global.com/e-resources/library-recommendation/?id=1

Related Content

Selective Pick-and-Place of Thin Film by Robotic Micromanipulation

Bruno Sauvet, Mohamed Boukhicha, Adrian Balan, Gilgueng Hwang, Dario Taverna, Abhay Shukla and Stéphane Régnier (2012). *International Journal of Intelligent Mechatronics and Robotics* (pp. 24-37).

www.igi-global.com/article/selective-pick-place-thin-film/71057?camid=4v1a

Ethical Treatment of Robots and the Hard Problem of Robot Emotions

Bruce J. MacLennan (2014). *International Journal of Synthetic Emotions* (pp. 9-16).

www.igi-global.com/article/ethical-treatment-of-robots-and-the-hard-problem-of-robot-emotions/113415?camid=4v1a

Mobile Laboratory Model for Next-Generation Heterogeneous Wireless Systems

Ibrahima Ngom, Hamadou Saliah-Hassane and Claude Lishou (2014). *Robotics: Concepts, Methodologies, Tools, and Applications* (pp. 1644-1661).

www.igi-global.com/chapter/mobile-laboratory-model-for-next-generation-heterogeneous-wireless-systems/84969?camid=4v1a

Core Methodologies in Data Warehouse Design and Development

James Yao, John Wang, Qiyang Chen and Ruben Xing (2013). *International Journal of Robotics Applications and Technologies* (pp. 57-66).

www.igi-global.com/article/core-methodologies-in-data-warehouse-design-and-development/95227?camid=4v1a